
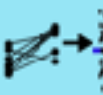


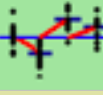



Common statistical tests are linear models

Last updated: 29 June, 2019. Also check out the [R version!](#)

See worked examples and more details at the accompanying notebook: <https://github.com/eigenfoo/tests-as-linear>

	Common name	Function in <code>scipy.stats</code>	Equivalent linear model in <code>smf.ols</code>	Exact?	The linear model in words	Icon
Simple Regression: ($y \sim 1 + x$)	y is independent of x P: One-sample t-test N: Wilcoxon signed-rank	<code>scipy.stats.ttest_1samp(y)</code> <code>scipy.stats.wilcoxon(y)</code>	<code>smf.ols("y ~ 1", data)</code> <code>smf.ols("y ~ 1", signed_rank(data))</code>	✓ for N > 14	One number (intercept, i.e., the mean) predicts y . - (Same, but it predicts the <i>signed rank</i> of y .)	
	P: Paired-sample t-test N: Wilcoxon matched pairs	<code>scipy.stats.ttest_rel(y1, y2)</code> <code>scipy.stats.wilcoxon(y1, y2)</code>	<code>smf.ols("y2_sub_y1 ~ 1", data)</code> <code>smf.ols("y2_sub_y1 ~ 1", signed_rank(data))</code>	✓ for N > 14	One intercept predicts the pairwise y₂-y₁ differences. - (Same, but it predicts the <i>signed rank</i> of y₂-y₁ .)	
	y ~ continuous x P: Pearson correlation N: Spearman correlation	<code>scipy.stats.pearsonr(x, y)</code> <code>scipy.stats.spearmanr(x, y)</code>	<code>smf.ols("y ~ 1 + x", data)</code> <code>smf.ols("y ~ 1 + x", rank(data))</code>	✓ for N > 10	One intercept plus x multiplied by a number (slope) predicts y . - (Same, but with <i>ranked x</i> and y)	
	y ~ discrete x P: Two-sample t-test P: Welch's t-test N: Mann-Whitney U	<code>scipy.stats.ttest_ind(y1, y2)</code> N/A in Python, but see R version <code>scipy.stats.mannwhitneyu(y1, y1)</code>	<code>smf.ols("y ~ 1 + group", data)^A</code> N/A in Python, but see R version <code>smf.ols("y ~ 1 + group", signed_rank(data))^A</code>	✓ ✓ for N > 11	An intercept for group 1 (plus a difference if group 2) predicts y . - (Same, but with one variance <i>per group</i> instead of one common.) - (Same, but it predicts the <i>signed rank</i> of y .)	
Multiple regression: ($y \sim 1 + x_1 + x_2 + \dots$)	P: One-way ANOVA N: Kruskal-Wallis	<code>scipy.stats.f_oneway(a, b, c)</code> <code>scipy.stats.kruskal(a, b, c)</code>	<code>smf.ols(y ~ 1 + G₂ + G₃ + ... + G_N)^A</code> <code>smf.ols(rank(y) ~ 1 + G₂ + G₃ + ... + G_N)^A</code>	✓ for N > 11	An intercept for group 1 (plus a difference if group ≠ 1) predicts y . - (Same, but it predicts the <i>rank</i> of y .)	
	P: One-way ANCOVA	N/A in Python, but see R version	<code>smf.ols("y ~ 1 + G₂ + G₃ + ... + G_N + X", data)^A</code>	✓	- (Same, but plus a slope on x .) <i>Note: this is discrete AND continuous. ANCOVAs are ANOVAs with a continuous x.</i>	
	P: Two-way ANOVA	N/A in Python, but see R version	<code>smf.ols("y ~ 1 + G₂ + G₃ + ... + G_N + S₂ + S₃ + ... + S_K + G₂*S₂+G₃*S₃+...+G_N*S_K", data)</code>	✓	Interaction term: changing sex changes the y ~ group parameters. <i>Note: G₂ to N is an indicator (0 or 1) for each non-intercept levels of the group variable. Similarly for S₂ to K for sex. The first line (with G_i) is main effect of group, the second (with S_i) for sex and the third is the group × sex interaction. For two levels (e.g. male/female), line 2 would just be "S₂" and line 3 would be S₂ multiplied with each G_i.</i>	[Coming]
	Counts ~ discrete x N: Chi-square test	<code>scipy.stats.chisquare(data)</code>	Equivalent log-linear model <code>sm.GLM(y ~ 1 + G₂ + G₃ + ... + G_N + S₂ + S₃ + ... + S_K + G₂*S₂+G₃*S₃+...+G_N*S_K, family=...)^A</code>	✓	Interaction term: (Same as Two-way ANOVA.) <i>Note: Run glm using the following arguments: glm(model, family=poisson()) As linear-model, the Chi-square test is log(y_i) = log(N) + log(a_i) + log(β_i) + log(a_iβ_i) where a_i and β_i are proportions. See more info in the accompanying notebook.</i>	Same as Two-way ANOVA
	N: Goodness of fit	<code>scipy.stats.chi2_contingency(data)</code>	<code>sm.GLM(y ~ 1 + G₂ + G₃ + ... + G_N, family=...)^A</code>	✓	(Same as One-way ANOVA and see Chi-Square note.)	1W-ANOVA

List of common parametric (P) non-parametric (N) tests and equivalent linear models. The notation $y \sim 1 + x$ is R shorthand for $y = 1 \cdot b + a \cdot x$ which most of us learned in school. Models in similar colors are highly similar, but really, notice how similar they *all* are across colors! For non-parametric models, the linear models are reasonable approximations for non-small sample sizes (see "Exact" column and click links to see simulations). Other less accurate approximations exist, e.g., Wilcoxon for the sign test and Goodness-of-fit for the binomial test. The signed rank function is `signed_rank(df) = np.sign(df) * df.rank()`. The variables G_i and S_i are "dummy coded" indicator variables (either 0 or 1) exploiting the fact that when $\Delta x = 1$ between categories the difference equals the slope. Subscripts (e.g., G_2 or y_1) indicate different columns in data. Im requires long-format data for all non-continuous models. All of this is exposed in greater detail and worked examples at <https://eigenfoo.xyz/tests-as-linear/>.

^A See the note to the two-way ANOVA for explanation of the notation.



Jonas Kristoffer Lindeløv, George Ho
<https://lindeloev.net>, <https://eigenfoo.xyz>